An Experimental Study of Communication and Coordination in Noncooperative Games*

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Received May 14, 1996

This paper reports the results of an experiment designed to test the usefulness of alternative solution concepts to explain players' behavior in noncooperative games with preplay communication. In the experiment subjects communicate by plain conversation prior to playing a simple game. In this setting, we find that the presumption of individualistic and independent behavior underlying the concept of Nash equilibrium is inappropriate. Instead, we observe behavior to be coordinated and correlated. Statistical tests reject Nash equilibrium as an explanation of observed play. The coalition proof correlated equilibrium of the game, however, explains the data when the possibility of errors by players is introduced. Journal of Economic Literature Classification Numbers: C72, C92.

*We are grateful to Mark Walker for his encouragement and for many helpful discussions, and to Doc Ghose for many valuable suggestions. Also we thank Jason Shachat, Vernon Smith, the associate editor and referees for useful comments, the Economic Science Laboratory at the University of Arizona for providing research support, the Ventana Corporation for authorizing the use of Groupsystems as the communication software in our experiment, and Doug Vogel for assisting us in the use of this software.

†This author gratefully acknowledges financial support from the Ministerio de Trabajo y Asuntos Sociales through funds administered by the Cátedra Gumersindo de Azcárate, and from DGICYT grant PB94-0378.

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1. INTRODUCTION

The solution concept used in most applications of noncooperative game theory is Nash equilibrium [Nash (1951)]. A mixed strategy profile is a Nash equilibrium if no player can increase his payoff by unilaterally changing his strategy. Thus, Nash equilibrium presumes that the players’ behavior is individualistic (i.e., only “individual” rather than “coordinated” or “coalitional” deviations are considered), and also that players choose their actions independently (i.e., they use “mixed” rather than “correlated” strategies).

This paper reports the results of an experiment designed to test whether these presumptions are appropriate when, as it is often the case in situations modelled as noncooperative games, preplay communication is possible, but binding agreements cannot be made. (In a Cournot oligopoly, for example, competitors may be unable to enforceably contract output levels due to antitrust regulation, although they may be able to freely discuss the outputs they intend to choose.) In the experiment subjects communicate by plain conversation prior to playing a simple game. In this setting, we find that the presumption of individualistic and independent behavior underlying the concept of Nash equilibrium is inappropriate. Instead, we observe behavior to be coordinated and correlated. Statistical tests reject Nash equilibrium as an explanation of observed play. The game has a correlated equilibrium which is immune to coalitional deviations, and which explains the data when the possibility of errors by players is introduced.¹

Our experimental results show that preplay communication introduces possibilities for coordination that may alter the outcome of a game in a fundamental way, and therefore that there is a need for solution concepts which account for these possibilities. Recently a number of such solution concepts were developed. These concepts presume that players coordinate their actions to their mutual benefit, although coordination is limited by the inability of players to commit. Among these, the concepts of strong Nash equilibrium (SNE) introduced by Aumann (1959), and coalition-proof Nash equilibrium (CPNE) developed by Bernheim et al. (1987) are perhaps best known.

A strategy profile is a SNE if no coalition of players by changing their strategies can make its members better off. Hence a SNE is invulnerable to any deviation by any coalition. The concept of strong Nash equilibrium may be too strong as it requires that an equilibrium be invulnerable even

¹To the best of our knowledge this experiment is the first providing empirical evidence of the play of a correlated equilibrium (which is not also a Nash equilibrium).
to deviations which are themselves vulnerable to further deviations. This problem with SNE was recognized by Bernheim et al. (1987), who proposed the notion of CPNE: A strategy profile is a CPNE if no coalition has a self-enforcing deviation which makes its members better off. A deviation is self-enforcing if no proper subcoalition of the deviating coalition has a further self-enforcing deviation which makes its members better off.

These solution concepts maintain the presumption that players choose their actions independently. When players can communicate, however, this presumption may not be appropriate. In the following game, which we refer to as the Three Player Matching Pennies Game (TPMG), coordination may give rise to correlated play.

Three players each simultaneously choose heads or tails. If all three faces match, then players 1 and 2 each win a penny while player 3 loses two pennies. Otherwise, player 3 wins two pennies while players 1 and 2 each lose a penny.

The matrix representation of the game is given in Table I below, where players 1, 2, and 3 choose, respectively, the row, the column, and the matrix.

In this game, players 1 and 2 have completely common interests (either they both win a penny or they both lose a penny), and their interests are completely opposed to those of player 3 (when they win, player 3 loses two pennies, and when they lose, player 3 wins two pennies). If players 1 and 2 can communicate, one might expect that they will coordinate their actions (i.e., they will both choose heads or both choose tails) as they lose whenever their actions do not match. When players 1 and 2 act as a “team,” the game effectively becomes the usual (two player) matching pennies game, which has a unique Nash (and unique correlated) equilibrium where each team chooses heads or tails with equal probability; i.e., with probability \( \frac{1}{2} \) players 1 and 2 both choose heads and with probability \( \frac{1}{2} \) both choose tails, while player 3 chooses heads or tails with equal probability. The resulting probability distribution over action profiles (i.e., correlated strategy) is given in Table II. As this probability distribution is not the

\[2\] Indeed, in many games (e.g., the prisoners’ dilemma) a SNE does not exist.

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<td>H</td>
<td>1, 1, −2</td>
<td>−1, −1, 2</td>
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<tr>
<td>T</td>
<td>−1, −1, 2</td>
<td>−1, −1, 2</td>
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\[1\]
product of its marginals, it cannot be generated by any mixed strategy profile. Thus, if players can communicate prior to play, one might not expect the players to choose their actions independently in this game.

Einy and Peleg (1995) (E & P) and Moreno and Wooders (1996) (M & W) develop notions of coalition-proof correlated equilibrium (CPCE) which not only presume that players coordinate their actions to their mutual benefit, but also allow correlated play. A CPCE is a correlated strategy from which no coalition has a self-enforcing deviation which makes its members better off. The notion of self-enforcingness used is the same as the one implicit in CPNE. Introducing the possibility of correlated play, however, makes it difficult to determine which deviations are feasible, and what is the appropriate criterion to use in deciding which deviations are improving. E & P and M & W take different approaches to resolving these difficulties, thereby obtaining different equilibrium notions. For the TPM PG, however, both equilibrium notions identify the correlated strategy in Table II as the game’s unique CPCE. Milgrom and Roberts (1996) recently extended Moreno and Wooders’ notion of CPCE to allow for the possibility that not all coalitions may be able to form, due perhaps to limited communication possibilities. Also Ray (1996) introduces a notion of coalition-proof correlated equilibrium. (We do not discuss this notion here since it presumes, unlike the notions of E & P and M & W, that players’ possibilities to correlate their play are limited to those achievable using an exogenously given correlating device.)

The paper is organized as follows. In Section 2 we discuss the experimental game and we study its equilibria. Section 3 discusses the experimental design. Section 4 describes the experimental results and performs

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**TABLE II**
The Coalition-Proof Nash Equilibrium of the Three Player Matching Pennies Game

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<th></th>
<th>H</th>
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<tbody>
<tr>
<td>H</td>
<td>(\frac{1}{4})</td>
<td>0</td>
</tr>
<tr>
<td>T</td>
<td>0</td>
<td>(\frac{1}{4})</td>
</tr>
</tbody>
</table>

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3Since deviations by a single player are always self enforcing, a CPCE must be a correlated equilibrium (see Aumann (1974) and (1987)). A correlated strategy is a correlated equilibrium if for every action profile which is selected with positive probability, no player, knowing only the action he is to play, can increase his expected payoff by taking a different action. The notion of correlated equilibrium admits the possibility of correlated play, although it maintains the presumption of individualistic behavior.
COMMUNICATION AND COORDINATION IN GAMES

Section 6 is devoted to testing for coordinated and correlated behavior and to testing whether observed play can be explained by any of the solutions concepts discussed when players make errors. Section 7 concludes.

2. EQUILIBRIA OF THE THREE PLAYER MATCHING PENNIES GAME

Our experimental game is the TPMG. This game is simple enough that equilibrium theory will have a good chance of succeeding in an experimental setting, yet the possibility of coordinated and correlated behavior play an important role. In this section we describe the equilibria of the TPMG.

Nash Equilibria and Coalition-Proof Nash Equilibria

The pure strategy profiles \((H, H, T)\) and \((T, T, H)\), and the mixed strategy profile where each player chooses heads or tails with equal probability are the only Nash equilibria of the TPMG. In each of the pure Nash equilibria players 1 and 2 each lose a penny, while player 3 wins two pennies. In the mixed strategy Nash equilibrium players 1 and 2 each obtain an expected payoff of \(-\frac{1}{2}\), while player 3's expected payoff is 1.

None of the Nash equilibria is a CPNE: In each of the pure strategy Nash equilibria, the coalition of players 1 and 2 by jointly deviating in order to "match" player 3's action—i.e., both choosing \(T\) in the equilibrium \((H, H, T)\), and both choosing \(H\) in the equilibrium \((T, T, H)\)—can each win a penny. Both deviations are self-enforcing as neither player 1 nor player 2 can gain by deviating further. Hence neither \((H, H, T)\) nor \((T, T, H)\) is a CPNE. The mixed Nash equilibrium is not a CPNE, as the deviation in which players 1 and 2 both choose \(T\) is also improving (players 1 and 2 obtain a payoff of 0) and self-enforcing. Therefore the TPMG has no CPNE since a CPNE must be a Nash equilibrium.4

Coalition-Proof Correlated Equilibria

We establish that the correlated strategy in Table II, denoted by \(p^*\), is a CPCE of the TPMG by showing that no coalition of players has an improving deviation. Clearly, neither player 1 nor player 2 can improve by

4A SNE is always a CPNE since a SNE is invulnerable to improving deviations, self-enforcing or otherwise, by any coalition of players. Thus, the TPMG does not have a SNE either.
unilaterally deviating, as they both lose whenever they choose different actions. In addition, given the strategies of players 1 and 2, player 3 obtains a payoff of zero regardless of the strategy he plays; therefore he cannot improve either by unilaterally deviating. Hence $p^*$ is a correlated equilibrium. Moreover, as player 3’s interests are completely opposed to those of players 1 and 2, no coalition of more than one player which includes player 3 has a deviation which is improving for all its members. Further, when player 3’s action is selected according to $p^*$, he chooses heads or tails with equal probability; hence players 1 and 2 obtain at most a payoff of zero from any deviation. Since they already obtain a payoff of zero when action profiles are selected according to $p^*$, the coalition of players 1 and 2 does not have an improving deviation either. Thus, $p^*$ is a CPCE of the TPM PG.

We now establish that although the set of correlated equilibria is large, the incentive constraints which guarantee that a correlated strategy is immune to coalitional deviations identify the correlated strategy $p^*$. Thus, any equilibrium theory based on the presumption that players coordinate their actions to their mutual benefit, and which allows correlated behavior should identify this strategy as the game’s unique equilibrium. Therefore, in addition to testing the notions of CPCE proposed by E & P and M & W, the present experiment provides a test for any equilibrium theory consistent with these premises.

Let $p$ be an arbitrary correlated equilibrium, i.e., immune to individual deviations, and write $p_{ijk}$ for the probability of action profile $(i, j, k) \in \{H, T\}$. Consider the (self-enforcing) deviation by the coalition of players 1 and 2 in which they both choose $H$ with probability one. When player 3 continues to choose his action according to $p$, then the probability that he chooses $H$ is $p_{HHH} + p_{HTH} + p_{THH} + p_{TTH}$; in this case players 1 and 2 each win a penny. In any other case (i.e., when player 3 chooses $T$) players 1 and 2 each lose a penny. Thus, if players 1 and 2 deviate to both choosing $H$, each obtains

$$U^D = p_{HHH} + p_{HTH} + p_{THH} + p_{TTH} - p_{HHT} - p_{HTT} - p_{THT} - p_{TTT}.$$ 

For $p$ to be immune to deviations of this kind it must satisfy $U^D \leq U_i^*(p) = U_i(p)$, where $U_i(p)$ denotes the expected payoff of player $i$ when actions are chosen according to $p$. For $p$ to be immune to the deviation in which players 1 and 2 both choose $T$ with probability one, $p$ must satisfy also $-U^D \leq U_i(p) = U_i(p)$. Therefore, we have $U_i(p) = U_i(p) \geq 0$. Further, $p$ must satisfy $U_i(p) \geq 0$ since otherwise it would not be immune to

\footnote{In fact, we have shown that $p^*$ is a “strong correlated equilibrium,” as it is immune to any deviation (self-enforcing or otherwise) by any coalition.}
the deviation in which player 3 chooses \( H \) and \( T \) with equal probability, independently of the choices of players 1 and 2—this deviation guarantees player 3 a payoff of zero. Since the game is zero sum, this implies \( U_i(p) = 0 \) for \( i = 1, 2, 3 \).

We now complete the argument that if \( p \) is immune to coalitional deviations, then \( p = p^* \). Since \( p \) is a correlated equilibrium, the incentive constraints for player 3 require \( p_{TTH} \geq p_{HHH} \) and \( p_{HHT} \geq p_{THT} \). These two inequalities and \( U_3(p) = 0 \) imply \( p_{TTH} = p_{HHH} \), \( p_{HHT} = p_{THT} \), and \( p_{HTH} = p_{HHT} = p_{THT} = 0 \). Using these probabilities to calculate \( U_1(p) \) and \( U_3(p) \), we have that \( U_1(p) \geq U_3(p) \) implies \( p_{TTT} \geq p_{TTH} \), and \( U_3(p) \geq -U_3(p) \) implies \( p_{HHH} \geq p_{HHT} \). Thus, we get

\[
P_{TTT} \geq p_{TTH} = p_{HHH} \geq p_{HHT} = p_{THT}.
\]

Because these probabilities must add up to one, we have \( p_{TTH} = p_{HHH} = p_{HHT} = p_{THT} = \frac{1}{4} \). Hence \( p = p^* \), and therefore \( p^* \) is the unique CPCE of the TPMPG.

3. EXPERIMENTAL DESIGN

In the version of the TPMPG played in the experiment, each player chose either circle or square. We adopted these labels for the strategies as the labels “Heads” and “Tails” are suggestive of randomization. A subject’s role in the game was indicated by one of the colors “Blue,” “Red,” or “White.” The game was described to the subjects as follows: If all three players choose the same figure (that is, if all three choose circle or all three choose square), then the Blue and the Red player each earn $7.50 and the White player earns $0. In any other case, the Blue and the Red player each earn $0 and the White player earns $15.00. Subjects played the game only once.

Subjects were recruited in groups of 12 for sessions lasting 1 hour.\(^6\) None of the subjects had previously participated in the experiment. Prior to the subjects entering the lab, 12 computers were “linked” by software to form four groups of three computers. Each subject was seated at one of these computers. The game was played anonymously as subjects did not know which computers where in the same group.

In order to provide the subjects with the rich communication opportunities presumed by the notions of coalition-proofness we discuss, each subject was able to communicate both publicly and privately with the other members of his group. Subjects used their computers to communicate for

\(^6\)In seven sessions only nine subjects participated due to “no shows.”
15 minutes before choosing their actions. To facilitate this communication, each subject's computer screen was divided into three windows. A label at the top of each window indicated which players could send messages to that window and which players could see that window's messages.

A Blue player, for example, had windows labelled “Blue–Red,” “Blue–White,” and “Blue–Red–White.” A Blue player could communicate privately with the Red (White) player in his group by exchanging messages in the Blue–Red (Blue–White) window. A Blue player communicated publicly through the Blue–Red–White window. The screen of a Blue player is displayed in Fig. 1.

The mechanics of exchanging messages were simple. To send a message to a particular window, a subject activated it by using his mouse to point and click on it. The subject then composed his message, which was displayed in the lower box of the window as it was typed. The message was sent when the subject used his mouse to point and click on the Submit button.

\footnote{A Red player had windows labelled Blue–Red, Red–White, and Blue–Red–White, while a White player had windows labelled Blue–White, Red–White, and Blue–Red–White.}

\begin{center}
\textbf{FIG. 1. A Blue player's screen.}
\end{center}
button at the bottom of the window. A message sent to a window was then displayed on the screens of all the players listed in the window’s label. A message sent to the Blue–Red window, for example, was displayed in the Blue–Red window of the screens of both the Blue and the Red player. Whenever a player sent a message, a tag was automatically attached which identified his color. The tag also indicated the hour and minute that the message was sent.

A transcript of players’ dialog in one of the sessions is given in Appendix B. In this transcript, the first message in the Blue–Red, Red–White, and Blue–Red–White windows were practice messages. The time spent exchanging these messages was not included in the 15 minutes of the communication phase.8 (Transcripts are available upon request.)

Anonymity

The solution concepts we discuss apply to situations where the players of the game cannot make binding agreements. Therefore, preserving the anonymity of subjects throughout the experiment was an essential feature of the experimental design. Had subjects not been anonymous, reneging on agreements would be costly and, in that case, agreements are no longer entirely nonbinding. Anonymity also had the important role of eliminating the possibility of credible promises of side payments. In order to preserve anonymity, subjects were instructed that they were not to send messages in which they identified themselves. They were also told that their messages would be monitored to insure that they did not identify themselves. No other constraints were placed on the content of messages.

Expected Utility and Expected Monetary Payoff

The TPMG has only two outcomes; either the figures of all three players are the same (a “win” for the Blue and the Red players and a “loss” for the White player), or they are not all the same (a win for the White player and a loss for the Blue and Red players). Therefore, provided that each player prefers the outcome where he wins (and obtains a higher monetary payoff in this case), and provided that each player’s preferences over lotteries can be represented by a von Neumann–Morgenstern utility function, we can take monetary payoffs to be utility payoffs. Since payoffs

8 Experimental games in which some subset of players has coincident interests, and therefore has an incentive to communicate truthfully, may be especially useful for experimental tests of a solution concept. In the TPMG, for example, examination of the transcripts allows us to obtain an insight into what the Blue and the Red players expect the White player to do, and how these players formulate a plan for communicating with the White player.
in the experimental game can be obtained by positive affine transforma-
tions of the payoffs of the version of the TPMPG presented in the
Introduction, the equilibria of these games are the same.

One-Shot

There are several reasons why one might want to avoid an experimental
design where the game is played repeatedly. First, once the game is
repeated, risk attitudes become relevant as risk averse players may have an
incentive to coordinate their play in a way which reduces the riskiness of
their payoffs. (As already noted, no assumption about the risk attitudes of
players is necessary for the one-shot game.) Second, repetition (with fixed
partners) raises the possibility of “renegotiation.” A version of CPCE
which accounts for renegotiation, and which is thus appropriate for dy-
namic games, has not yet been developed. Our design avoids these compi-
lcations, and thus makes the interpretation of our results clear. Of course,
in a one-shot design it is essential that the game be simple, since subjects
will not have the chance to “learn” the game by playing it repeatedly. The
TPMPG, however, is simple enough that we can be confident that it is
understood at first play. This issue is discussed further in Section 6, where
we test whether experience alters play.

4. The Experimental Data

Table III presents the empirical frequency of each action profile after 69
plays of the TPMPG.9 The number in parentheses below each frequency is
the number of times that profile was observed. In the game, each player
had two actions, circle (C) or square (S). An action profile is a triple

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<tr>
<td>C</td>
<td>S</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>0.261</td>
<td>0.072</td>
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<tr>
<td></td>
<td>(18)</td>
<td>(5)</td>
</tr>
<tr>
<td>S</td>
<td>0.014</td>
<td>0.188</td>
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<td></td>
<td>(1)</td>
<td>(13)</td>
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<tbody>
<tr>
<td>C</td>
<td>S</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>0.217</td>
<td>0.029</td>
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<td>(15)</td>
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<tr>
<td>S</td>
<td>0.029</td>
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9The frequencies do not add up to 1 due to rounding.
\((i, j, k)\) in the set \(\{C, S\}^3\) of possible action profiles, where \(i, j,\) and \(k\) denote, respectively, the action of the Blue (row), Red (column), and White (matrix) player. Blue and Red players won in 31 of 69 plays, a win frequency which is not significantly different from one half, the win frequency implied by the CPCE of the game. In the mixed Nash equilibrium this win frequency is only 25\%, and in either of the pure Nash equilibria it is 0\%. The hypothesis that this win frequency is 25\% is rejected for degrees of significance as small as 0.005. Of course, the hypothesis that this win frequency is 0\% is rejected at any level of significance. Blue players chose circle in 40 of the plays, while Red and White players chose circle in 36 and 37 plays, respectively. Each player’s frequency of circle is not, however, statistically significantly different from one half.

Next we investigate whether our data is consistent with the presumption of independent behavior underlying the concepts of Nash equilibrium, CPNE, and SNE. Our data can be regarded as a sequence of independent realizations of a multinomial random variable whose values are the elements of the set of possible action profiles. Different hypotheses about the data generating process can be framed as different restrictions on the multinomial distribution. Throughout we conduct hypothesis tests using the “likelihood ratio test.”

For each action profile \((i, j, k) \in \{C, S\}^3\), denote by \(p_{ijk}\) its probability. A sample can be represented by a vector \(n = (n_{ijk})_{ijk \in \{C, S\}^3}\), where each \(n_{ijk}\) is the number of times action profile \((i, j, k)\) was observed. Also denote by \(N\) the number of observations in a sample (i.e., \(N = \sum_{ijk \in \{C, S\}^3} n_{ijk}\)). The log of the likelihood that a sample \(n\) was generated by a multinomial distribution \(p = (p_{ijk})_{ijk \in \{C, S\}^3}\) is

\[
\ln(l(p)) = \ln a + \sum_{ijk \in \{C, S\}^3} n_{ijk} \ln p_{ijk},
\]

where \(a = N!/(\prod_{ijk \in \{C, S\}} n_{ijk})\).

We first consider the null hypothesis that in our sample all three players chose their actions independently against the alternative hypothesis that they did not (i.e., that the sample was generated by an arbitrary multinomial distribution).\(^{10}\) Under the null hypothesis, the likelihood attains its maximum at \(\hat{p}_{ijk}^0 = (n_i, n_j, n_k)/N^3\), where \(n_i, n_j,\) and \(n_k\) are, respectively, the number of times that Blue players chose action \(i\), Red players

\(^{10}\)We test for independence using maximum likelihood ratio tests, rather than using a simpler goodness of fit test, since maximum likelihood techniques will become necessary for our later analysis.
chose action $j$, and White players chose action $k$. Under the alternative hypothesis, the likelihood attains its maximum at $\hat{p}_{ijk} = n_{ijk}/N$. The likelihood ratio, given by

$$-2\left( l\left( \hat{p}_{ijk}^0 \right) - l\left( \hat{p}_{ijk}^1 \right) \right),$$

is asymptotically distributed as chi-square with 4 degrees of freedom. The degrees of freedom are the difference between the dimension of the parameter space under the alternative hypothesis (7 in this case) and under the null hypothesis (3 in this case). Tests of pairwise independence are constructed in a similar fashion [see, e.g., Mood et al. (1974)].

The results of likelihood ratio tests of independence of players' actions are given in Table IV below. The column $\chi^2_{0.05}$ provides a value such that if the likelihood ratio exceeds this value, then the null hypothesis is rejected at the 0.05 significance level; the number in parentheses indicates the degrees of freedom of the chi-square.

The hypothesis that the actions of all three players are independent is rejected at the 0.05 significance level. In fact, it is rejected for significance levels as small as 0.005. The source of this rejection is the apparent correlation in the actions of Blue and Red players; the hypothesis that the Blue and Red players choose their actions independently is rejected at significance levels as small as 0.005. The hypotheses of pairwise independence between Blue and White and between Red and White are not rejected at the 0.05 level of significance.

Although these results are inconsistent with the presumption of independence implicit in the concept of Nash equilibrium, on the basis of these tests alone one cannot conclude that observed behavior is not the result of Nash equilibrium play. Different Nash equilibria in different plays of the game could lead to the appearance of correlation, even if actions in any

<table>
<thead>
<tr>
<th>Null: Independence of players' actions</th>
<th>$\chi^2_{0.05}$</th>
<th>Likelihood ratio</th>
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<tbody>
<tr>
<td>Blue–Red–White</td>
<td>9.49 (4)</td>
<td>40.71</td>
</tr>
<tr>
<td>Blue–White</td>
<td>3.84 (1)</td>
<td>0.58</td>
</tr>
<tr>
<td>Red–White</td>
<td>3.84 (1)</td>
<td>0.02</td>
</tr>
<tr>
<td>Blue–Red</td>
<td>3.84 (1)</td>
<td>339.70</td>
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</table>
given play were independent. In Section 6 we test this hypothesis. The results of the tests of independence, however, are consistent with the prediction of CPCE that Blue and Red players correlate their actions, and that the actions of Blue and Red players are uncorrelated with the actions of White players.

The presumption that players coordinate their actions to their mutual benefit implies for the TPM PG that Blue and Red players choose the same figure. Indeed, this occurred in 59 plays. Nonetheless, Blue and Red players “failed to coordinate” in 10 of the 69 plays, which is inconsistent with CPCE.

Examining the transcripts provides some insight into the sources of coordination failures. The most common source of coordination failures is Blue or Red players proposing, in the Blue–Red window, a last-minute change in the figure to be chosen (this seems to explain four of the observed coordination failures). Such a proposal by a Blue player, for example, left the Red player uncertain of how to play. The second most common cause of coordination failures was a player choosing a figure different from the one he agreed to choose (this was the case in three plays). One coordination failure seemingly was due to a player’s failure to understand the game; another coordination failure occurred when the entire communication phase was consumed discussing the strategy of play, thereby leaving the Blue and the Red players no time to select a figure to coordinate on. Only one coordination failure seems to have been due to Blue and Red players failing to recognize the benefits of coordination. We note also that in two plays the Blue and Red players fail to recognize the benefits of coordination, yet choose the same figure, resulting in “unexpected” coordination successes. We conclude that explaining player behavior requires accounting for the possibility that players make errors. In the next section we present a model of play in the TPM PG which admits this possibility.

5. THE THREE PLAYER MATCHING PENNIES GAME WITH ERRORS

In experimental settings there are a number of elements that might lead a player to choose an action different from the one he intended: a player may misunderstand the rules of the experimental game, or he may simply make an error. In our experiment, there is also the possibility that a player’s choice of an action may be based on a “miscommunication” (i.e., a message may be misinterpreted, the source of a message may be confused, or a message may be sent to a player different from the one intended). A
theory which ignores the possibility of errors might be rejected, even though it correctly predicts “intended behavior.”

We introduce the possibility of errors into the TPM PG by assuming that when a player selects a figure, with probability $1 - \epsilon$ he chooses the figure he intended, but with probability $\epsilon$ he chooses a figure randomly (i.e., he chooses “square” or “circle” with equal probability). We assume that all players make errors with the same probability, that the errors of players are independent, and that the error structure is common knowledge.

The TPM PG combined with errors by players yields a new game which we denote by TPM PG($\epsilon$). In this new game, a pure strategy for a player is interpreted as the action he intends to play. The payoff of each player for each profile of intended actions is given in Table V below, where $w = 7.5\rho_w(\epsilon)$, and $l = 7.5\rho_l(\epsilon)$. The term $\rho_w(\epsilon) = 1 - \frac{3}{2}\epsilon + \frac{3}{8}\epsilon^2$ is the probability that all the players choose the same figure when all the players intend to choose the same figure, and $\rho_l(\epsilon) = \frac{3}{4}\epsilon - \frac{1}{2}\epsilon^2$ is this probability when one of the players intends to choose a figure different from the figure of another player. For error rates $\epsilon$ less than one, the payoffs in the TPM PG($\epsilon$) can be obtained by positive affine transformations of the payoffs in the original TPM PG, and therefore the equilibria of these games are the same.

In the TPM PG($\epsilon$) it is necessary to make a distinction between intended actions and actual actions (i.e., the actions that are observed). The probability distribution over intended actions is generally different from the probability distribution over actual actions, the latter distribution depending on the error rate. Thus, although the equilibria of the TPM PG and TPM PG($\epsilon$) are the same, the probability distributions over profiles of actual actions corresponding to these equilibria are generally different. (An exception is the mixed Nash equilibrium.) Henceforth denote by $\theta_k = (\epsilon/2)^k(1 - (\epsilon/2))^{3-k}$, the probability that exactly $k$ players choose an action different from the one intended.

<table>
<thead>
<tr>
<th></th>
<th>$C$</th>
<th>$S$</th>
<th>$C$</th>
<th>$S$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C$</td>
<td>$w, w,(15 - 2w)$</td>
<td>$l, l,(15 - 2l)$</td>
<td>$C$</td>
<td>$l, l,(15 - 2l)$</td>
</tr>
<tr>
<td>$S$</td>
<td>$l, l,(15 - 2l)$</td>
<td>$l, l,(15 - 2l)$</td>
<td>$S$</td>
<td>$l, l,(15 - 2l)$</td>
</tr>
</tbody>
</table>
Each of the Nash equilibria gives rise to a probability distribution over actual action profiles of the form given in Table VI below. The probabilities \( \rho_k \) differ for each of the equilibria: when the players intend to play the pure strategy Nash equilibrium \((S, S, C)\), then \( \rho_k = \theta_k \); when they intend to play the pure strategy Nash equilibrium \((C, C, S)\), then \( \rho_k = \theta_{3-k} \); finally, if the players intend to play the mixed strategy Nash equilibrium, then \( \rho_k = \frac{1}{3} \).

Coalition-Proof Nash Equilibrium of the Three Player Matching Pennies Game with Errors

In the CPCE of the TPMPG(\( \epsilon \)), with probability \( \frac{1}{2} \) the Blue and the Red players both intend to choose square and with probability \( \frac{1}{2} \) they both intend to choose circle, while the White player intends to choose each figure with equal probability. The probability distribution over actual action profiles is given in Table VII, where \( \delta = \epsilon(1 - (\epsilon/2)) \) is the probability that the Blue and the Red players fail to coordinate their actions. Unlike the probability distribution over intended action profiles (see Table II), the probability distribution over actual action profiles gives each outcome a positive probability. Hence when players make errors, the likelihood of any finite sample is positive under the hypothesis that players play the CPCE of the game. Thus, we can no longer automatically reject this hypothesis if there is a coordination failure.

---

The labels \( C \) and \( S \) in this table now represent actual (i.e., observed) actions, whereas in Table III they represented intended actions.

---

### Table VI
Nash Equilibria in the Three Player Matching Pennies Game (\( \epsilon \))

<table>
<thead>
<tr>
<th></th>
<th>( C )</th>
<th>( S )</th>
<th>( C )</th>
<th>( S )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( C )</td>
<td>( \rho_2 )</td>
<td>( \rho_1 )</td>
<td>( \rho_2 )</td>
<td>( \rho_1 )</td>
</tr>
<tr>
<td>( S )</td>
<td>( \rho_1 )</td>
<td>( \rho_0 )</td>
<td>( \rho_2 )</td>
<td>( \rho_1 )</td>
</tr>
</tbody>
</table>
TABLE VII
Coalition-Proof Nash Equilibrium in the Three Player Matching Pennies Game

<table>
<thead>
<tr>
<th></th>
<th>C</th>
<th>S</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>4δ</td>
<td>4δ</td>
</tr>
<tr>
<td>S</td>
<td>4δ</td>
<td>4δ</td>
</tr>
</tbody>
</table>

6. TESTS OF HYPOTHESES IN THE THREE PLAYER MATCHING PENNIES GAME WITH ERRORS

In this section we analyze the experimental data in the context of the $\text{TPM PG}(\epsilon)$. We test the underlying assumptions of the alternative solution concepts (i.e., independent versus correlated behavior, and individualistic versus coordinated behavior), and also we test alternative equilibrium theories. Finally, we discuss the results of experiments designed to test whether experience reduces the frequency of errors. We begin by deriving the likelihood function for each of the hypotheses of interest.

Independent Behavior

In Section 4 we reported the results of tests of independence of the players' (actual) actions. The presumption of independence in the $\text{TPM PG}(\epsilon)$ pertains to players intended actions rather than to their actual play. It is easy to check, however, that since players make errors independently, whenever players intend to choose their actions independently, then actual actions are also independent. Hence incorporating the possibility that players make errors does not increase the maximum likelihood under the hypothesis of independence, and the results of tests of independence for the $\text{TPM PG}(\epsilon)$ are the same as those reported in Section 4 for the $\text{TPM PG}$.

Coordinated Play

As we noted in Section 4, the presumption that players coordinate their actions to their mutual benefit would lead Blue and Red players always to choose the same action. Thus, under the null hypothesis of coordinated behavior, intended actions are selected according to a multinomial distri-


bution \( p = (p_{ijk})_{ijk \in \{C,S\}} \) satisfying

\[ P_{CCC} + P_{CCS} + P_{SSC} + P_{SSS} = 1. \]

In this case, actual actions are selected according to the multinomial \( \bar{p} \) given by

\[
\bar{p}_{ijk} = p_{ijk} \theta_0 + (p_{-ijk} + p_{i-j-k} + p_{i-j-k}) \theta_1 \\
+ (p_{-i-j-k} + p_{-i-j-k} + p_{i-j-k}) \theta_2 + p_{i-j-k} \theta_3,
\]

where \( \neg r = S \) if \( r = C \), and \( \neg r = C \) if \( r = S \). The likelihood of our data under the hypothesis that Blue and Red players coordinate their actions is obtained by replacing these probabilities in Eq. (\ast).

**Nash Equilibrium**

Since the TPMPG has multiple Nash equilibria, an appropriate test for whether our data was generated by Nash equilibrium play must allow the possibility that observed play is the result of a “mixture” of Nash equilibria. When the pure strategy Nash equilibria \((S,S,C)\) and \((C,C,S)\) generated a proportion \( \lambda_1 \) and \( \lambda_2 \) of the observed plays, respectively, and the mixed Nash equilibrium generated the remaining observed plays, the probability distribution over actual actions is of the form in Table VI, where

\[ \rho_k = \lambda_1 \theta_k + \lambda_2 \theta_{3-k} + (1 - \lambda_1 - \lambda_2) \frac{1}{3}. \]

From this multinomial distribution one can calculate the log likelihood function using Eq. (\ast). For our data this function is

\[ l^{NE}(\lambda_1, \lambda_2, \epsilon) = \ln a + 13 \ln \rho_0 + 19 \ln \rho_1 + 22 \ln \rho_2 + 15 \ln \rho_3. \]

**Coalition-Proof Correlated Equilibrium**

The probability distribution over actual action profiles that results when players choose their actions according to the CPCE of the TPMPG(\(\epsilon\)) is described in Table VII. Given a sample \( n \), denote by \( N_F \) the number of observations where the Blue and the Red players fail to coordinate their actions (i.e., \( N_F = n_{CSC} + n_{SCS} + n_{SCS} + n_{CSS} \)). Using Eq. (\ast), one can
calculate the log likelihood that the observed data was generated by the CPCE of the game as

$$f^{CPCE}(\epsilon) = \ln a + N_F \ln \frac{\delta}{4} + (N - N_F) \ln \frac{1 - \delta}{4}. $$

For our sample, $N_F = 10$ and $N = 69$.

Results

The results of our tests are presented in Table VIII below. The first row contains the maximum likelihood estimate of the error rate and the value of the likelihood ratio under the null hypothesis that Blue and Red players coordinated their actions. At the 0.05 significance level we fail to reject this null hypothesis. Thus, the presence of coordination failures in our data can be explained as the result of players’ errors.

The second row contains the maximum likelihood estimate of the error rate and the value of the likelihood ratio under the null hypothesis that the data was generated by a mixture of the three Nash equilibria, against the alternative that the data was generated by some arbitrary multinomial distribution. According to the likelihood ratio test, this null hypothesis is rejected at the 0.05 level of significance; in fact, it is rejected for levels of significance as small as 0.005. Although we do not report the tests here, each of the null hypotheses that the data was generated by the mixed or either of the pure Nash equilibria of the game is also rejected.

The third row of Table VIII shows the results of the maximum likelihood estimation of the error rate, and the value of the likelihood ratio under the null hypothesis that the data was generated by the CPCE of the

<table>
<thead>
<tr>
<th>Null hypothesis</th>
<th>$\chi^2_{0.05}$</th>
<th>$\hat{\epsilon}$</th>
<th>Likelihood ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coordinated play</td>
<td>7.82 (3)</td>
<td>0.1592</td>
<td>3.16</td>
</tr>
<tr>
<td>Mixture of NE $^b$</td>
<td>9.49 (4)</td>
<td>0.5437</td>
<td>34.61</td>
</tr>
<tr>
<td>CPCE</td>
<td>12.59 (6)</td>
<td>0.1573</td>
<td>4.42</td>
</tr>
</tbody>
</table>

$^a$The parameter estimates are $\hat{\rho}_{CCC} = 0.32$, $\hat{\rho}_{CCS} = 0.22$, and $\hat{\rho}_{SSC} = 0.22$. These estimates were obtained using Gauss. The standard errors of these estimates are, respectively, 0.067, 0.058, and 0.060; the standard error of the estimated error rate is 0.051.

$^b$The parameter estimates are $\hat{\lambda}_1 = 0.4493$ and $\hat{\lambda}_2 = 0.5507$, with standard errors of, respectively, 0.0891 and 0.0891; the standard error of the estimated error rate is 0.0863.
The maximum likelihood estimator of the error rate is

\[ \hat{e} = 1 - \sqrt{1 - 2 \left( \frac{N_F}{N} \right)} . \]

(The second order condition for a maximum is that \( N_F < N/2 \), a condition which is satisfied by our data.) According to the likelihood ratio test we fail to reject this hypothesis at the 0.05 significance level. In fact, we fail to reject this hypothesis for significance levels as large as 0.5.

The failure to reject the null hypothesis that the data was generated by the CPCE of the TPM PG(\( e \)) against the alternative that it was generated by an arbitrary multinomial distribution is very robust with respect to the error rate. The curve in Fig. 2 below shows the value of the likelihood ratio as a function of the error rate. A horizontal line was drawn at the value 12.59. A chi-square with 6 degrees of freedom is less than 12.59 with probability 0.95. At a 0.05 significance level, we fail to reject the null hypothesis that the data was generated by the CPCE of the TPM PG(\( e \)) for a large range of error rates (any rate in the interval [0.054, 0.353]).

It is worth pointing out that at the 0.05 significance level we do not reject the null hypothesis that the data was generated by the CPCE of the game against the alternative hypothesis that it was generated by an arbitrary correlated equilibrium. Denoting the maximum value of the log likelihood under the null and alternative by \( l^{CPCE} \) and \( l^{CE} \), the likelihood ratio for this test satisfies

\[ -2(l^{CPCE} - l^{CE}) \leq -2(l^{CPCE} - l^{A}) = 4.42, \]

FIG. 2. Likelihood ratio for CPCE as a function of \( e \).
where $l^A$ is the maximum value of the log likelihood under the hypothesis that the data is generated by an arbitrary multinomial. (The inequality follows from the fact that $l^{CE} \leq l^A$ since the hypothesis that the data was generated by an arbitrary correlated equilibrium is more restrictive than it having been generated by an arbitrary multinomial. Likelihood ratio values are taken from Table VIII.) Also under the alternative that the data was generated by a correlated equilibrium, the parameter space has a dimension no less than three as there are at least four linearly independent correlated equilibria (the three Nash equilibria and the CPCE); therefore the likelihood ratio is asymptotically distributed as a chi-square with $k \geq (3 - 1)$ degrees of freedom. Thus,

$$
\chi^2_{0.05}(k) \geq \chi^2_{0.05}(2) = 5.99 > 4.42 \geq -2(l^{CPCE} - l^{CE}),
$$

and hence we fail to reject the null that the data was generated by the CPCE against the alternative that it was generated by an arbitrary correlated equilibrium.

We continue to reject the null hypothesis that the data was generated by a mixture of the Nash equilibria even with the more restrictive alternative that the data was generated by an arbitrary correlated equilibrium. The likelihood ratio for this test satisfies

$$
-2(l^{NE} - l^{CE}) = -2(l^{NE} - l^A) + 2(l^{CE} - l^A)
$$

$$
\geq -2(l^{NE} - l^A) + 2(l^{CPCE} - l^A)
$$

$$
= 34.61 - 4.42 = 30.19.
$$

(The inequality follows from the fact that $l^{CE} \leq l^{CPCE}$. On the other hand, the likelihood ratio is asymptotically distributed as a chi-square with $k \leq 7 - 3$, as the dimension of the parameter space under the alternative hypothesis is no greater than 7. The result follows since $30.19 > 9.49 = \chi^2_{0.05}(4) \geq \chi^2_{0.05}(k)$.

**Experience and Errors**

Although our statistical tests support the CPCE of the TPM PG(e) as an explanation of observed behavior, the frequency of coordination failures in our data might be regarded as “high.” This seemingly high frequency of coordination failures might have been due to the subjects’ lack of experience with the game, as they played the game only once. In order to test whether experience reduces the frequency of coordination failures, we ran five sessions in which 12 subjects played the TPM PG three times.\textsuperscript{12} After

\textsuperscript{12} Subjects were told that they were going to play the game “several times” (they were not informed of how many), each time with different partners.
each play, a subject was informed of his earnings for that play and the choices of the other members of his group. Subjects were then rematched so that no two subjects were members of the same group more than once. Each of these sessions therefore produced four first plays, four second plays, and four third plays. Table IX below presents the results of these experiments; each entry $n_{ijk}^1 - n_{ijk}^2 - n_{ijk}^3$ indicates the number of times action profile $ijk \in \{C, S\}^3$ was observed in, respectively, the first, the second and the third play.

Testing whether experience leads to fewer coordination failures amounts to testing whether experience reduces error rates. Note that the data reported in Table III as well as the data for first plays reported in Table IX correspond to observed play of “inexperienced” subjects. Thus, provided that the changes in the experimental design under which these new observations were generated were not significant, it is appropriate to pool this data. We therefore test the null hypothesis that the data reported in Table III and the data for first plays reported in Table IX are drawn from the same multinomial distribution against the alternative that they are drawn from different multinomials. The likelihood ratio for this test is 5.71 and therefore we fail to reject this null at the 0.05 significance level since $5.71 < \chi^2_{0.05}(7) = 14.1$.

In order to test for an experience effect, we therefore pool the data in Table III and the data for first plays in Table IX. We also pool the data for subsequent plays, i.e., second and third plays. We then test the null hypothesis that the error rate for first plays (89 observations) and the error rate for subsequent plays (40 observations) are the same against the alternative that they differ. (In each case, maintaining that intended play is governed by the CPCE.) Since the likelihood ratio for this test is 4.564 >

13Neither can we reject the null hypothesis that error rates for the data in Table III and for first play data in Table IX are the same against the alternative that they differ, when we maintain that intended play is governed by the CPCE.

### Table IX

<table>
<thead>
<tr>
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<th>C</th>
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<th>C</th>
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<td></td>
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<td>S</td>
<td></td>
<td>C</td>
<td>S</td>
</tr>
<tr>
<td></td>
<td>8-7-6</td>
<td>0-0-0</td>
<td></td>
<td>4-8-7</td>
<td>1-0-0</td>
</tr>
<tr>
<td>C</td>
<td>1-0-0</td>
<td>3-2-2</td>
<td></td>
<td>0-0-1</td>
<td>3-3-4</td>
</tr>
<tr>
<td>S</td>
<td></td>
<td></td>
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<td></td>
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</tr>
</tbody>
</table>


$\chi^2_{0.05}(1) = 3.84$, we reject this null.\(^\text{14}\) (The estimated error rate under the null is 0.1064, while under the alternative the estimated error rate is 0.1454 for first plays and 0.0253 for subsequent plays.) Thus experience leads to lower error rates.

**Summary**

In summary, our experimental data supports the presumption of coordinated play, and it strongly rejects the presumption of independent behavior. Moreover, it supports the hypothesis that the data was generated by play of the CPCE of the game, while it clearly rejects the hypothesis of Nash equilibrium play. We should note also that although the experiment does not allow one to test the predictive power of the notions of coalition-proof Nash equilibrium or strong Nash equilibrium (neither type of equilibrium exists for the TPMG), it provides some evidence against these notions as both presume that players chose their actions independently. In addition, neither identifies a coalition-proof equilibrium even though there is an intuitively compelling one, the CPCE of the game, which is supported by the data.

7. CONCLUSIONS

The results of our experiment stress the importance of accounting for coordinated play in noncooperative games with preplay communication. Moreover, the experiment strongly suggests that the players’ attempt to realize mutual gains naturally leads to correlated play. Indeed, in many applications of noncooperative games the situations under study are ones where the players have rich opportunities to communicate prior to play. In these applications, the use of Nash equilibrium as “the” solution concept may not be appropriate. Instead, one should investigate the behavior predicted by solution concepts that account for the possibilities for coordination there might be. More stringent experimental tests of such concepts would consider games in which the equilibrium does not call for the players to choose each of their actions with equal probability. Such a strategic situation is more complex and it seems likely that experience may play a greater role than in the present experiment. We regard a full examination of these issues as being an interesting direction for further research.

\(^{14}\)At the 0.05 significance level, the critical value for the alternative that the error rate for subsequent plays is lower than for first plays is 2.71, therefore leading to a stronger rejection of the null.
An alternative approach to dealing with preplay communication is to transform the game, introducing explicitly any opportunities to communicate the players might have. There are two potential difficulties with this approach: First, it might simply be infeasible when opportunities to communicate are rich and unstructured. (With “plain conversation,” for example, there is no prespecified order in which messages may be sent and no restriction on the content of messages.) Second, even when communication opportunities are limited and structured, and therefore they can be modeled explicitly, taking the Nash equilibria of the transformed game as the prediction of play ignores the possibilities for coordinated play that communication might bring about. Moreover, this approach leads to very weak predictions: For any Nash equilibrium of the original game there is a Nash equilibrium of the transformed game where the players choose their messages arbitrarily and then, ignoring all messages, choose their actions according to a Nash equilibrium of the original game.

A feasible and perhaps more practical approach is to devise solution concepts which account for communication opportunities implicitly. Moreover, this approach might lead to stronger predictions. In the TPM PG, for example, there is a continuum of correlated equilibria, but only one CPCE.

APPENDIX A: INSTRUCTIONS

To control for the possibility that the order of the presentation of the examples may introduce bias in the play, we used two sets of instructions which differed in the order the examples were presented, but did not differ in any other respect. We could not reject the hypothesis that the data generated using different sets of instructions came from the same probability distribution.

Instructions

If at any time you have a question as I go through these instructions, please raise your hand. During this experiment, you may not speak to other participants.

In this experiment, you and the other participants have been divided into groups of three players. You will play a simple game with the other two members of your group. In every group there is one Blue, one Red, and one White player. (Please turn over the envelope at your station. The color of the sticker on the envelope at your station tells you which type of player you are.) Your monetary earnings from playing the game are determined by your color and the choices made by the players in your group.

You will play the game only once!
Communication

Before making your choice, you will have the opportunity to communicate with the other members of your group. You communicate by using your computer to send and to receive messages. To help you do this, the screen in front of you is divided into three windows. You can send messages to any of these windows. The label at the top of a window tells you which players in your group can see that window’s messages. In order to show you how you can send messages, you will send a practice message.

Instructions for Blue Players

If you are a Blue player, your screen displays the three windows shown on the overhead. These windows are labelled Blue–Red, Blue–White, and Blue–Red–White. (If you are a Blue player and your screen does not show these windows, please raise your hand.)

You can send messages to any window on your screen. Only you and the Red player in your group can see messages in the Blue–Red window. Only you and the White player in your group can see messages in the Blue–White window. All three players in your group can see messages in the Blue–Red–White window.

You will now send a practice message to the Red player (but not the White player) in your group. If you are a Blue player, please do the following.

1. Use your mouse to point and click on the lower box in the Blue–Red window;
2. type "Hi, this is a message to Red."
3. Use your mouse to point and click on the Submit button at the bottom of the Blue–Red window.

Your screen now appears as displayed on the overhead. The message you just typed is displayed in your Blue–Red window.

You can send messages to White (but not to Red) from the Blue–White window, and you can send messages to both Red and White from the Blue–Red–White window.

Instructions to Red Players

If you are a Red player, your screen displays windows labelled Blue–Red, Red–White, and Blue–Red–White, as shown in the overhead. (If you are a Red player and your screen does not show these windows, please raise your hand.)
Notice that the message just typed by the Blue player appears in your Blue–Red window. At the end of the message is a label which identifies Blue as the sender of the message.

You will now send a practice message to the White player (but not the Blue player) in your group. If you are a Red player, please do the following.

1. Use your mouse to point and click on the lower box in the Red–White window;
2. type "Hi, this is a message to White."
3. Use your mouse to point and click on the Submit button in the Red–White window.

Your screen now appears as displayed on the overhead. Your message to White is displayed in your Red–White window.

You can send messages to Blue but not to White from the Blue–Red window, and you can send messages to both Blue and White from the Blue–Red–White window.

Instructions to White Players

If you are a White player, your screen should display the three windows shown in the overhead. The windows are labelled Blue–White, Red–White, and Blue–Red–White. If you are a White player and your screen does not show these windows, please raise your hand.

Notice that the message just typed by the Red player appears in your Red–White window.

You will now send a practice message to both the Blue and the Red player in your group. If you are a White player, please do the following.

1. Use your mouse to point and click on the lower box in the Blue–Red–White window
2. type "Hi, this is a message to both the other players."
3. Use your mouse to point and click on the Submit button in the Blue–Red–White window.


You can send messages to Blue (but not to Red) from the Blue–White window, and you can send messages to Red (but not to Blue) from the Red–White window.
In this experiment you will remain anonymous. As preserving anonymity is important, you may not send messages that in any way identify yourself. You may not, for example, send a message which gives your name or your phone number. The messages you send will be monitored in order to ensure that you do not identify yourself.

The Game: Choices and Earnings

If you have a question as I read through the remaining instructions, please raise your hand and a monitor will approach you to answer your question.

Please open the envelope at your station. Inside you will find a sheet of paper. On the side labelled “Record Sheet,” please copy the number on your bingo ball in the space for “Subject ID.” Keep the ball as it is the only way in which we can identify you.

I will now describe the game that you play with the other members of your group. In the game, each player chooses either circle or square. Your earnings are determined according to the following rules:

- If all three players in your group choose the same figure (that is, if all three choose circle or all three choose square), then
  - Blue earns $7.50.
  - Red earns $7.50.
  - White earns $0.

- If any player in your group chooses a figure different from another player, then
  - Blue earns $0.
  - Red earns $0.
  - White earns $15.

These rules are summarized by the following table. (A copy of this table is on the other side of your record sheet.)

<table>
<thead>
<tr>
<th>Choices</th>
<th>Earnings</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blue</td>
<td>Red</td>
</tr>
<tr>
<td>○</td>
<td>○</td>
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<tr>
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</tbody>
</table>
If all the players in your group choose circle, then all have chosen the same figure. The first row of the table shows that, in this case, Blue earns $7.50, Red earns $7.50, and White earns $0. If Blue chooses square, Red chooses circle, and White chooses square then all three players have not chosen the same figure. The last row shows that, in this case, Blue and Red each earn $0 and White earns $15.

If you have any questions regarding how your earnings are determined, please raise your hand now.

The experiment proceeds as follows.

- Before making your choice, you will have 15 min. to communicate with the other members of your group.
- After 15 min., you will make your choice.
- Once earnings are computed you will be called by your subject ID, one person at a time, to collect your earnings. At that time you will be told the choices of the other players in your group.
- You will then immediately exit the lab.

**REMEMBER:** You will play the game only once and you may not send messages which identify yourself.

If you have any questions, please raise your hand now.

[Subjects communicated for 15 min.]

The communication phase is now over. Please turn off your monitor.

- Please make your choice by checking either the circle or the square on your record sheet.
- Put your record sheet back into the envelope.

[Record sheets were collected.]

While we determine your earnings, we ask you to take a short quiz to test whether you understand how your earnings are determined.

- Write your subject ID on the quiz where indicated.
- For the given choices, write the earnings of each player. Your answers to the quiz will not affect your earnings.

[Quizzes were collected.]

Please wait at your station until your subject ID is called.

- When you are called, take your bingo ball to the back of the room to collect your earnings.
- After you are paid, please exit the laboratory.
**APPENDIX B: TRANSCRIPT**

**Players’ Actions: (C,S,S)**

<table>
<thead>
<tr>
<th>Blue-Red</th>
<th>Blue-White</th>
<th>Red-White</th>
<th>Blue-Red-White</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Hi, this is a message to Red.</strong> (5/23/95, 2:16 PM, Blue)</td>
<td><strong>“Hi this is a message to White”</strong> (5/23/95, 2:18 PM, Red)</td>
<td><strong>“Hi, this is a message to both the other players”</strong> (5/23/95, 2:19 PM, White)</td>
<td></td>
</tr>
</tbody>
</table>

| We have to choose the same one and convince White to also (5/23/95, 2:27 PM, Blue) | What do you think we should do? (5/23/95, 2:27 PM, White) | I really have no idea, you have the best chance to win (5/23/95, 2:28 PM, Blue) | **What do you think we should do?** (5/23/95, 2:28 PM, White) |

| How do we do that (5/23/95, 2:28 PM, Red) | **What do you think we should do?** (5/23/95, 2:27 PM, White) | What do you think we should do? (5/23/95, 2:28 PM, White) |

| Tell White that we are picking a circle so he will probably pick a circle thinking that we are tricking him. (5/23/95, 2:29 PM, RED) | **Won’t he think that is reverse psychology anyway?** (5/23/95, 2:30 PM, Blue) | **Maybe it will work** (5/23/95, 2:30 PM, Blue) | **Should I tell him we’re picking circle?** (5/23/95, 2:31 PM, Blue) |

| **If we tell him we are picking a circle he will think we are picking a square and pick the circle so we should pick the circle** (5/23/95, 2:32 PM, Red) | **Ok I’ll do it on the open channel** (5/23/95, 2:32 PM, Blue) |

| Now what do you think he’ll think (5/23/95, 2:33 PM, Blue) | **What are you going to pick** (5/23/95, 2:33 PM, Red) | We’re going to pick circle (5/23/95, 2:33 PM, Blue) |

| He is probably trying to figure out what we are really picking (5/23/95, 2:34 PM, Red) | **What are you going to pick** (5/23/95, 2:33 PM, Red) | I f both of you try to put the same thing you have a 50/50 chance of winning $7.50 each considering that I put the opposite. However, if I just put whatever I want, I can win $15 (5/23/95, 2:34 PM, White) |

| So we’re definitely picking circle, right? (5/23/95, 2:34 PM, Blue) | **What do you think we should do?** (5/23/95, 2:27 PM, White) | What do you think we should do? (5/23/95, 2:28 PM, White) |

**Hi this is a message to Red.** (5/23/95, 2:16 PM, Blue)
right there is 50/50 chance, basically he doesn't know what we're picking, what if he thinks we are really picking the circle, he doesn't know about reverse psychology.

Maybe not! Now we have to figure out what he thinks. Should we change our minds to him for a bit of confusion and still pick circle? 

Maybe we should pick the square, I can't decide now.

Why don't we pass messages back and forth on the open and directly to him for part of the rest of the time and still pick the same one, but with all our messages there's still a 50/50 chance.

How are you doing? My best chance of winning is to choose circle or square without letting you know, so I think that's what I'm going to do. Good luck with your guess of what I'm going to pick. If you have anything to say just write back.

I'm doing great. Thank goodness we don't know anyone else in the group, huh?

Let's do it privately then on the direct to white channel.

So do we pick square? What do you mean, let's pick the circle.

Ok.
REFERENCES


